

# Restricted Numeral Systems and the Hunter-Gatherer Connection

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# Numerals are

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- **spoken**
- **normed expressions** that are used to denote the
- **exact number** of objects for an
- **open class of objects** in an
- **open class of social situations** with
- **the whole speech community** in question

# Restricted Numeral Systems: Definition

A numeral system is *restricted* iff

1. Monomorphemic numerals exist only up to 2 or 3 AND
  2. Higher quantities are expressed orally only
    - a) inexactly or
    - b) up to ca 10 with additions of 1, 2 and 3 (possibly including ad hoc use of 'hand' for 5).
- Example: !Kū (Juu, Botswana-Namibia) of Vedder (1910-1911):

1	ē
2	dsã
3	!gao
viel	!gao

# Restricted Numeral Systems: Notes

- A numeral system with normed usage of hand + feet for 5, 10, 20 will never be called a “restricted” numeral system.
- People with restricted numeral systems may use one or more of the following strategies to cope with higher quantities:
  1. Do without exact counting above 3 and live happily anyway
  2. Use hands, fingers and feet for tallying in an ad-hoc way
  3. Use hands, fingers and feet in a normed way (but without corresponding oral expressions)
  4. Use numerals from another language
  5. Keep track of things by tallying or individuizing

# History of Research

- Probably the earliest descriptions of restricted numeral system come from the Americas:

**Taino of Hispaniola (Arawakan):** (Very unclear)

Ramón Pané 1571 [1498] Relación acerca de las antigüedades de los indios

**Tupinambá (Tupian):** (Rather Unclear)

Joseph de Anchieta 1595 [1556] Arte de Grammatica da Lingoa mais usada na costa do Brasil

Jean de Lery 1578 Histoire d'un voyage fait en la terre du Bresil, avtrement dite Amerique

- Probably the first scholars to mention restricted numeral systems in contrast to others are

**Re Tupinamba** Locke 1689 An essay concerning human understanding

**Re Thracians – probably erroneous** and Leibniz 1697 Unvorgreifliche Danken

- 19th-20th century scholars frequently flash the label “primitive” but do little to understand the nature and distribution of restricted numeral systems

# Worldwide Presence of Restricted Systems

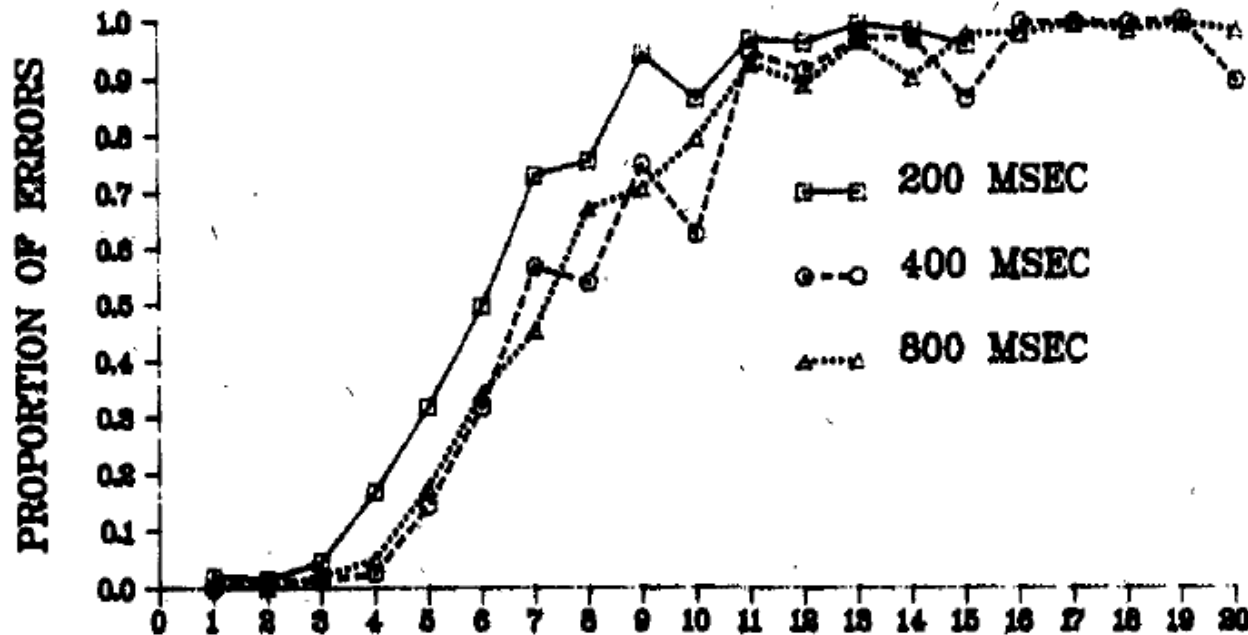
- Out of 6 880 languages in the world for which there is published data on numerals
- 1 093 languages are attested with a restricted system

Note:

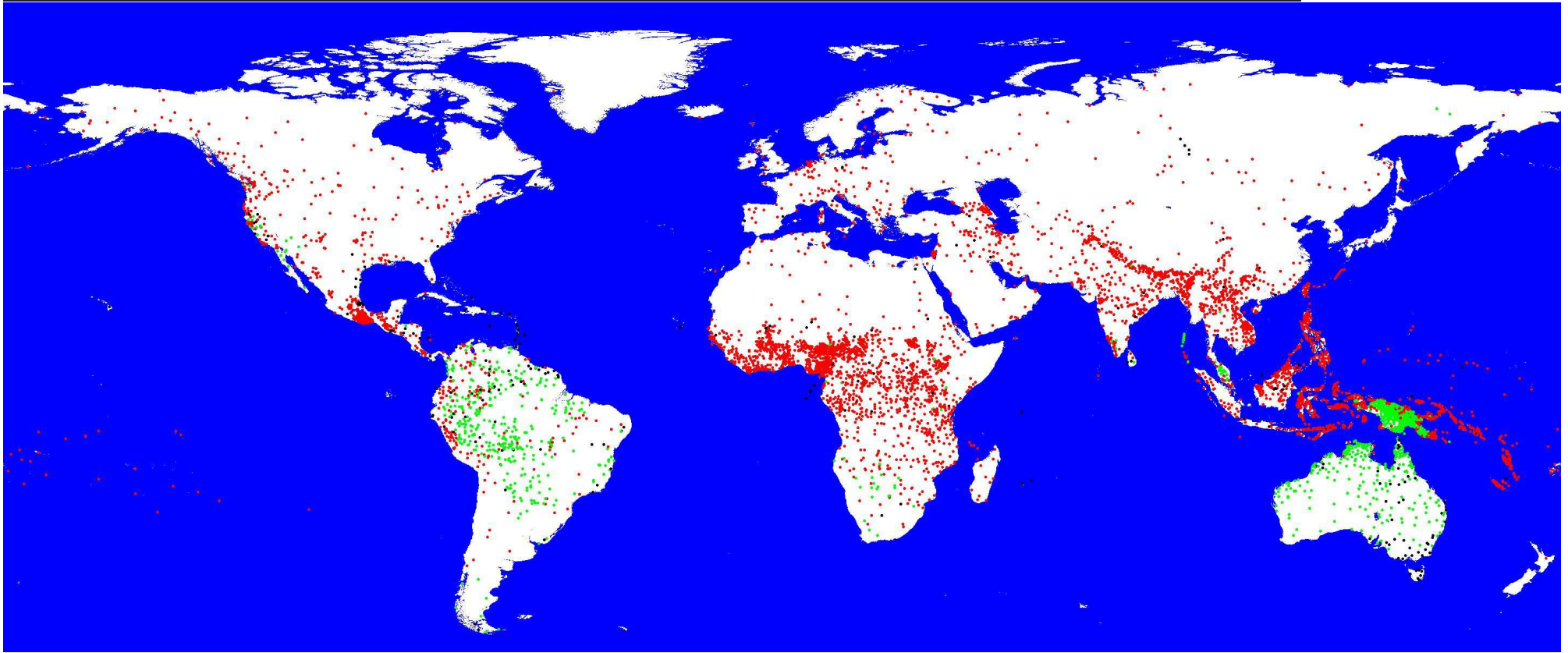
- There are no bona fide cases of languages with “almost restricted” numeral systems, say, numerals up to, e.g., 5, 6, 10, 13.
- Not all restricted numeral systems are necessarily alike:
  - Most end at 2, many end at 3
  - Ca 15 cases where the 2-word is claimed to mean ‘a few’ (Papua, Amazon)
  - 2 cases with very good evidence that both the 1-word and 2-word are fuzzy: Pirahã and Ninam (Yanomami, Brazil)

# Whence Restricted Numeral Systems?

- A limit at 2-3 coincides with the cognitively established **subitizing limit** =  
the number of objects one immediately sees how many they are, without grouping or counting.
- George Mandler and Billie J. Shebo 1982 Subitizing: An analysis of its component processes, p 8:



# Geographical Distribution





# Restricted Systems and Hunter-Gatherers

A language is a Hunter-Gatherer (HG) language iff

its speakers subsist more than 50% on plants and animals whose reproduction is not controlled by humans

- Amendment 1: If a language

- with known HG-status ethnographically

- borrows numerals 3+ or 4+

⇒ then it had an original restricted numeral system

- Amendment 2: If a language *family*

- with known HG-status ethnographically

- can reconstruct numerals up to exactly 2 or exactly 3 (inclusive)

⇒ then it had an original restricted numeral system

- Amendment 3: If a language
  - is not directly attested with a restricted system in vocabularies
  - but there ethnographic evidence that they are “unable to count beyond 3”

⇒ then it has a restricted numeral system

- Maes, Josef. (1947) Belgisch-Kongo, p 722  
Der Ituri-urwäld Pygmäe kann kaum bis drei zählen.
- Hose, Charles & William McDougall. (1912) The pagan tribes of Borneo, V2 p 193:  
The most striking evidence of the low cultural standing of the Punan is the fact that he cannot count beyond three (the words are 'ja', 'dua', 'telo'); all larger numbers are for him merely many 'pina'.
- Shortt, John. (1865) An Account of Some Rude Tribes, the Supposed Aborigines of Southern India, p 380:  
[Re Yenadies of Strihurreecottah] One or two of the boys, with the exception of a few errors, could count up to a hundred. Most of them, even with the assistance of their fingers, could not add numbers together; some could not tell how much three and two were, and the brightest among them could not add two figures to make twelve.

# Worldwide HG Survey: Numbers

To count independent cases of restricted systems:

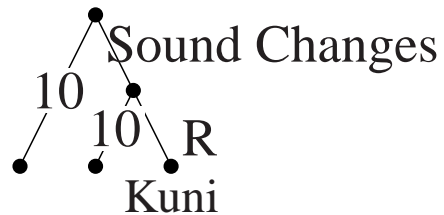
- If the phylogenetic history of the numeral system of a family is known, this gives which occurrences are independent
- Otherwise, look at every restricted system with independent *forms*

	Restricted	Restricted-Amendment	Non-Restricted
HG	85	35	76
NON-HG	7	1	124

- The poorly populated cell is non-HG & Restricted system  
If a language has a restricted system, then the speakers are likely HG

# Restricted → HG Covariation

- Several language families have some AGR and some HG member languages where the HG languages have restricted systems and the AGR members have non-restricted systems: Austroasiatic (Minor Mlabri, Hill Korwa), Cushitic, Morehead and Upper Maro, Pygmies (Ubangi, Bantu, Central Sudanic), Austronesian (Negritos, Tasaday, To Ala, Punan, Sera-Sissano, Waropen, Kuni), Chibchan, Khoe-Kwadi
- Shrinking must be inferred in the cases such as:
  - Kuni (Austronesian/Oceanic, Papua New Guinea):



- Minor Mlabri (Austroasiatic/Khmuic, Thailand): Old Khmuic numeral morphemes are preserved in ritual formulae

# Why Restricted Systems?

Why all AGR languages, as well as some HG languages, invent non-restricted systems is not well-understood:

- HG societies typically have many uses for exact counting, e.g.:

- Valiente-Noailles, Carlos. (1993) *The Kua: Life and Soul of the Central Kalahari Bushmen*, p 87:

- She ... wait for the moment of birth ... calculate the nine month period ... counting the moons

- Number of days to a festivity

- Lots of evidence for non-verbal counting

- There is no simple explanation involving *trade*

- Trade is omnipresent in HG societies around the world

- \* Thurnwald, Richard. 1932 *Economics in primitive communities*. OUP.

- \* Micha, Franz Josef. (1958) *Der Handel der Zentralaustralischen Eingeborenen*. *Annali Lateranensi* XXII. 41-228.

- Expressions for exact numbers are **not** a pre-requisite for trade, e.g., a Spanish-Panare trade pidgin has a restricted system where 'vente' means 'many'

- Riley, Carroll L. (1952) *Trade Spanish of the Piñaguero Panare*. *Studies in Linguistics* 10(1). 6-11.

# **Restricted Systems in Khoisan**

**Sandawe (AGR) :** Not restricted (5-10-100)

**Hadza (HG) :** Restricted plus Datooga + Swahili loans

**Kx'a :**

**Ju (HG) :** Restricted

**Amkhoe (HG) :** Restricted

**Tuu :**

**!Ui (HG) :** Attested languages restricted (possible exception //Xegwi?)

**Lower Nosop (HG) :** Restricted

**Taa (HG) :** Restricted

**Khoe-Kwadi :** See next slide

# **Khoe-Kwadi**

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**Kwadi (PAS)** : Not restricted

**Khoe** :

**Khoekhoe** :

**North** :

**Hai//om (HG)** : Not restricted / Borrowings from Nama?

**Nama (AGR)** : Not restricted

**Bergdama (HG)** : Restricted

**South (AGR)** : Not restricted

**Non-Khoekhoe** :

**Ts'ixa (HG)** : Restricted

**Ost-Kxoe** :

**Shua (HG)** : **Some lects restricted, some not**

**Tshwa (HG)** : Restricted

**West-Kxoe** :

**Khwe-//Ani** :

**Khwe (HG)** : Restricted

**//Ani (HG)** : **probably not restricted**

**Naro-Ana** :

**Naro (HG)** : Originally restricted

**//Gana (HG)** : Restricted

**/Gwi (HG)** : Restricted

# Khoe-Kwadi 1-4

	Capelo/Ivens 1886 Westphal (nd) Kwadi	Nienaber 1962:37 Nama 1626	Hagman 1977 Nama	Heine 1999:37   Ani	Vossen 2013:216 Cara   Xaise   Danisi			Wilhelm 1955:26 Khwe
1	wí	istwee	/gui	/úí	/úí	/úí	/úí	/gúichā
2	ám	istum	/gam	/ám	/ám	/ám	/ám	/gǎm
3	dátùà < Bantu	istgwunny	!nona	n!òànà	//óbé	ngónà	//óbé	!nōǎǎ
4	né < Bantu	hackey	haka	fàtsâ	hàtsá	//óbé	-	-

- 1-4 reconstructs to proto-Khoe:

=> no inference from numerals that proto-Khoe was HG

- 1-2 only shared between proto-Khoe and Kwadi:

? => proto-Khoe-Kwadi was HG, or

? => Kwadi went through a HG stage between the split from proto-Khoe-Kwadi and the present



**The End**

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Thank You for Listening!

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- Vossen, R. (2013). Shua. In Vossen, R., editor, *The Khoesan languages*, Routledge Language Family Series, pages 71–73, 103–104, 215–227, 401–407. London & New York: Routledge.
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